

SYSTEMS OF TWO EQUATIONS IN TWO VARIABLES



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UNIQUE SOLUTION

Point of intersection between the lines

INFINITE SOLUTIONS

Lines coincide

NO SOLUTION

Lines do not intersect

Methods to solve systems of equations:
Graphing, Elimination, Equal Values, Substitution, Determinants, and Matrix.

GRAPHING METHOD: Solve the following system of equations:

$$2x + y = 5 \text{ ----- } \textcircled{1}$$

$$3x - y = 0 \text{ ----- } \textcircled{2}$$

1) Isolating "y" from each equation:

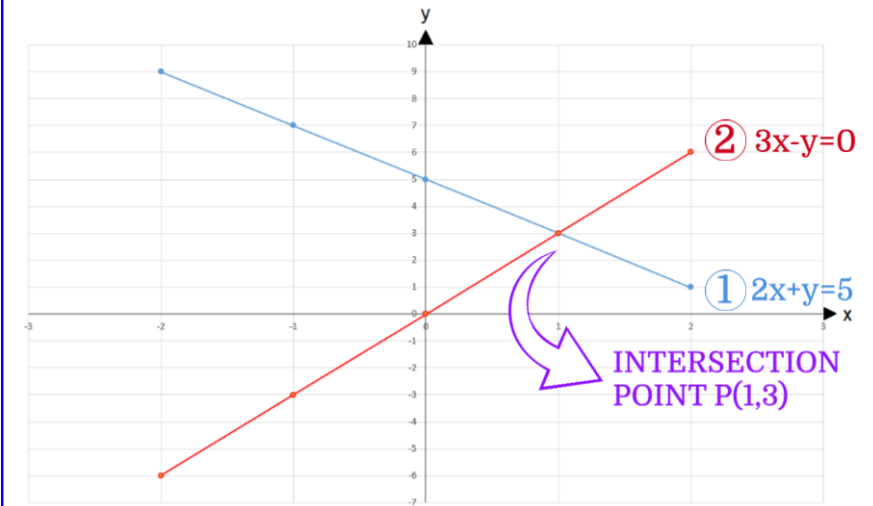
$$y = 5 - 2x \text{ ----- } \textcircled{1}'$$

$$y = 3x \text{ ----- } \textcircled{2}'$$

2) Tabulating $\textcircled{1}'$ and $\textcircled{2}'$:

$\textcircled{1}'$ $y=5-2x$			$\textcircled{2}'$ $y=3x$		
x	y	P(x,y)	x	y	P(x,y)
-2	$y=5-2(-2)=9$	P(-2,9)	-2	$y=3(-2)=-6$	P(-2,-6)
-1	$y=5-2(-1)=7$	P(-1,7)	-1	$y=3(-1)=-3$	P(-1,-3)
0	$y=5-2(0)=5$	P(0,5)	0	$y=3(0)=0$	P(0,0)
1	$y=5-2(1)=3$	P(1,3)	1	$y=3(1)=3$	P(1,3)
2	$y=5-2(2)=1$	P(2,1)	2	$y=3(2)=6$	P(2,6)

3) Graphing $\textcircled{1}'$ and $\textcircled{2}'$:



VERIFICATION: Because $x=1$; $y=3$, substitute in:

$\textcircled{1}$ $2x + y = 5$ $2(1)+3=5$ $2+3=5$ $5=5$	$\textcircled{2}$ $3x - y = 0$ $3(1)-3=0$ $3-3=0$ $0=0$
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Since "both" equalities are satisfied, we conclude that the SOLUTION is correct.



SYSTEMS OF TWO EQUATIONS IN TWO VARIABLES

ELIMINATION METHOD: Consists of eliminating one of the variables by adding or subtracting both equations.

ELIMINATION METHOD: Solve the following system of equations:

$$2x + y = 5 \text{ ----- } \textcircled{1}$$

$$3x - y = 0 \text{ ----- } \textcircled{2}$$

1) **Eliminating "x"**: we multiply $\textcircled{1}$ by (3) and $\textcircled{2}$ by (-2):

$$6x + 3y = 15 \text{ ----- } \textcircled{1}'$$

$$-6x + 2y = 0 \text{ ----- } \textcircled{2}'$$

2) Adding $\textcircled{1}'$ with $\textcircled{2}'$:

$$6x + 3y = 15$$

$$-6x + 2y = 0$$

$$5y = 15$$

$$y = 3$$

3) **Eliminating "x"**: adding $\textcircled{1}$ with $\textcircled{2}$:

$$2x + y = 5$$

$$3x - y = 0$$

$$5x = 5$$

$$x = 1$$

Hence, the solution point is $P(x,y)=P(1,3)$.

EQUAL VALUES METHOD: Consists in isolating a variable from both equations, and set them equal to each other to form a new equation of a single variable

EQUAL VALUES METHOD: Solve the following system of equations:

$$2x + y = 5 \text{ ----- } \textcircled{1}$$

$$3x - y = 0 \text{ ----- } \textcircled{2}$$

1) Isolating "y":

$$y = 5 - 2x \text{ ----- } \textcircled{1}'$$

$$y = 3x \text{ ----- } \textcircled{2}'$$

2) Equal values between $\textcircled{1}'$ and $\textcircled{2}'$ and isolating "x":

$$5 - 2x = 3x$$

$$x = 1$$

3) Isolating "x":

$$x = \frac{5 - y}{2} \text{ ----- } \textcircled{1}''$$

$$x = \frac{y}{3} \text{ ----- } \textcircled{2}''$$

4) Equal values between $\textcircled{1}''$ and $\textcircled{2}''$:

$$\frac{5 - y}{2} = \frac{y}{3}$$

$$y = 3$$

Hence, the solution point is $P(x,y)=P(1,3)$.

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KNOWLEDGE FOR THE WORLD



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SUBSTITUTION METHOD: Implies isolating a variable to be substituted into the other equation.

SUBSTITUTION METHOD: Solve the following system of equations:

$$2x + y = 5 \text{ ----- } \textcircled{1}$$

$$3x - y = 0 \text{ ----- } \textcircled{2}$$

1) Isolating "y" from $\textcircled{1}$:

$$y = 5 - 2x \text{ ----- } \textcircled{1}'$$

2) Substituting $\textcircled{1}'$ in $\textcircled{2}$ and solving:

$$3x - (5 - 2x) = 0$$

$$x = 1$$

3) Substituting $x=1$ in $\textcircled{2}$ and solving:

$$3(\textcircled{1}) - y = 0$$

$$y = 3$$

Hence, the solution point is $P(x,y)=P(1,3)$.

DETERMINANT: The determinant of a 2x2 matrix is the real number (Δ) calculated as:

$$\Delta = \begin{vmatrix} a & b \\ c & d \end{vmatrix} = ad - cb$$

DETERMINANTS METHOD: Calculate the determinant of the system (Δ_s), the determinant of "x" (Δ_x), and the determinant of "y" (Δ_y). Then:

$$x = \frac{\Delta_x}{\Delta_s} \wedge y = \frac{\Delta_y}{\Delta_s}$$

EXAMPLE: Solve the following system of equations by the **Determinants method**:

$$2x+y=5 \text{ ----- } \textcircled{1}$$

$$3x-y=0 \text{ ----- } \textcircled{2}$$

1) Calculating the determinant of the system:

$$\Delta_s = \begin{vmatrix} 2 & 1 \\ 3 & -1 \end{vmatrix} = (2)(-1) - (3)(1) = -2 - 3 = -5$$

2) Calculating the determinant of "x":

$$\Delta_x = \begin{vmatrix} 5 & 1 \\ 0 & -1 \end{vmatrix} = (5)(-1) - (0)(1) = -5 - 0 = -5$$

3) Calculating the determinant of "y":

$$\Delta_y = \begin{vmatrix} 2 & 5 \\ 3 & 0 \end{vmatrix} = (2)(0) - (3)(5) = 0 - 15 = -15$$

$$x = \frac{\Delta_x}{\Delta_s} \Rightarrow x = \frac{-5}{-5} \Rightarrow x = 1$$

$$y = \frac{\Delta_y}{\Delta_s} \Rightarrow y = \frac{-15}{-5} \Rightarrow y = 3$$

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